## 1981 AB 1 Calculator allowed for PART C ONLY

1. Let $f$ be the function defined by $f(x)=x^{4}-3 x^{2}+2$.
(a) Find the zeros of $f$.
(b) Write an equation of the line tangent to the graph of $f$ at the point where $x=1$.
(c) Find the $x$-coordinate of each point at which the line tangent to the graph of $f$ is parallel to the line $y=-2 x+4$.

1981 AB 6-BC 4 Calculator allowed
2. A particle moves along the $x$-axis so that at time $t$ its position is given by $x(t)=\sin \left(\pi t^{2}\right)$ for $-1 \leq t \leq 1$.
(a) Find the velocity at time $t$.
(b) Find the acceleration at time $t$.
(c) For what values of $t$ does the particle change direction?
(d) Find all values of $t$ for which the particle is moving left.

1990 AB 1 Calculator allowed
3. A particle initially at rest moves along the $x$-axis so that its acceleration at any time $t \geq 0$ is given by $a(t)=12 t^{2}-4$. The position of the particle when $t=1$ is $x(1)=3$.
(a) Find the values of $t$ for which the particle is at rest.
(b) Write an expression for the position $x(t)$ of the particle at any time $t \geq 0$.
(c) Find the total distance traveled by the particle from $t=0$ to $t=2$.

1988 AB 5 Calculator allowed
4. Let $R$ be the region in the first quadrant under the graph of $y=\frac{x}{x^{2}+2}$ for $0 \leq x \leq \sqrt{6}$.
(a) Find the area of $R$.
(b) If the line $x=k$ divides $R$ into two regions of equal area, what is the value of $k$ ?
(c) What is the average value of $y=\frac{x}{x^{2}+2}$ on the interval $0 \leq x \leq \sqrt{6}$ ?

## 1997 AB 3 No Calculator

5. Let $f$ be the function given by $f(x)=\sqrt{x-3}$.
(a) Sketch the graph of $f$ and shade the region $R$ enclosed by the graph of $f$, the $x$-axis, and the vertical line $x=6$.
(b) Find the area of the region $R$ described in part (a).
(c) Rather than using the line $x=6$ as in part (a), consider the line $x=w$, where $w$ can be any number greater than 3 . Let $A(w)$ be the area of the region enclosed by the graph of $f$, the $x$-axis, and the vertical line $x=w$. Write an integral expression for $A(w)$.
(d) Let $A(w)$ be described in part (c). Find the rate of change of $A$ with respect to $w$ when $w=6$.

## 1991 AB 5

6. Let $f$ be a function that is even and continuous on the closed interval $[-3,3]$. The function $f$ and its derivatives have the properties indicated in the table below.

| $x$ | 0 | $0<x<1$ | 1 | $1<x<2$ | 2 | $2<x<3$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 1 | Positive | 0 | Negative | -1 | Negative |
| $f^{\prime}(x)$ | Undefined | Negative | 0 | Negative | Undefined | Positive |
| $f^{\prime \prime}(x)$ | Undefined | Positive | 0 | Negative | Undefined | Negative |

(a) Find the $x$-coordinate of each point at which $f$ attains an absolute maximum value or an absolute minimum value. For each $x$-coordinate you give, state whether $f$ attains an absolute maximum or an absolute minimum.
(b) Find the $x$-coordinate of each point of inflection on the graph of $f$. Justify your answer.
(c) Sketch the graph of a function with all the given characteristics of $f$.

## 1989 AB 5



Note: This is the graph of the derivative of $f$, not the graph of $f$
7. The figure above shows the graph of $f^{\prime}$, the derivative of a function $f$. The domain of $f$ is the set of all real numbers $x$ such that $-10 \leq x \leq 10$.
(a) For what values of $x$ does the graph of $f$ have a horizontal tangent?
(b) For what values of $x$ in the interval $(-10,10)$ does $f$ have a relative maximum? Justify your answer.
(c) For what values of $x$ is the graph of $f$ concave downward? Justify your answer.
8. The graph of the function $f$ consists of a semicircle and two line segments as shown above. Let $g$ be the function given by $g(x)=\int_{0}^{x} f(t) d t$.

(a) Find $g(3)$.
(b) Find all values of $x$ on the open interval $(-2,5)$ at which $g$ has a relative maximum. Justify your answer.
(c) Write an equation for the line tangent to the graph of $g$ at $x=3$.
(d) Find the $x$-coordinate of each point of inflection of the graph of $g$ on the open interval $(-2,5)$. Justify your answer.

## 2004 AB 4 (Form B)

9. The figure below shows the graph of $f^{\prime}$, the derivative of the function $f$, on the closed interval $-1 \leq x \leq 5$. The graph of $f^{\prime}$ has horizontal tangent lines at $x=1$ and $x=3$. The function $f$ is twice differentiable with $f(2)=6$.
(a) Find the $x$-coordinate of each of the points of inflection of the graph of $f$. Give a reason for your answer.
(b) At what value of $x$ does $f$ attain its absolute minimum value on the closed interval $-1 \leq x \leq 5$ ? At what value of $x$ does $f$ attain its absolute maximum value on the closed interval $-1 \leq x \leq 5$ ? Justify your answers.
(c) Let $g$ be the function defined by $g(x)=x f(x)$. Find an equation for the line tangent to the graph of $g$ at $x=2$.


Graph of $f^{\prime}$


1999 AB 5
10. The graph of the function $f$, consisting of three line segments, is given above. Let $g(x)=\int_{1}^{x} f(t) d t$.
(a) Compute $g(4)$ and $g(-2)$.
(b) Find the instantaneous rate of change of $g$, with respect to $x$ at $x=1$.
(c) Find the absolute minimum value of $g$ on the closed interval [-2, 4]. Justify your answer.
(d) The second derivative of $g$ is not defined at $x=1$ and $x=2$. How many of these values are $x$-coordinates of points of inflection of the graph of $g$ ? Justify your answer.

